Let's begin with the equations for supply and demand:

Demand: 
$$Q_D = a - bP$$

Supply: 
$$Q_S = c + dP$$

We must choose numbers for a, b, c, and d.

■ Step 1:

Recall:

$$E = (P/Q)(\Delta Q/\Delta P)$$

For linear demand curves, the change in quantity divided by the change in price is constant (equal to the slope of the curve).



Substituting the slopes for each into the formula for elasticity, we get:

$$E_D = -b(P*/Q*)$$

$$Es = d(P * /Q *)$$

■ Since we will have values for  $E_D$ ,  $E_S$ ,  $P^*$ , and  $Q^*$ , we can solve for b & d, and a & c.

$$QD^* = a - bP^*$$

$$QS^* = c + dP^*$$

- Deriving the long-run supply and demand for copper:
  - The relevant data are:
    - $\bullet$  Q\* = 7.5 mmt/yr.
    - ◆P\* = 75 cents/pound
    - $\bullet E_S = 1.6$
    - $\bullet E_D = -0.8$

$$\blacksquare E_s = d(P^*/Q^*)$$

$$= 1.6 = d(75/7.5)$$
 $= 0.1d$ 

$$d = 1.6/0.1 = 16$$

$$E_d = -b(P^*/Q^*)$$

$$-0.8 = -b(.75/7.5)$$
  
= -0.1b

$$b = 0.8/0.1 = 8$$



■ Supply = 
$$Q_S^* = c + dP^*$$

$$-7.5 = c + 16(0.75)$$

$$7.5 = c + 12$$

$$c = 7.5 - 12$$

$$c = -4.5$$

$$Q = -4.5 + 16P$$

■ Demand = 
$$Q_D^* = a - bP^*$$

$$\blacksquare$$
 7.5 =  $a$  -(8)(.75)

$$7.5 = a - 6$$

$$a = 7.5 + 6$$

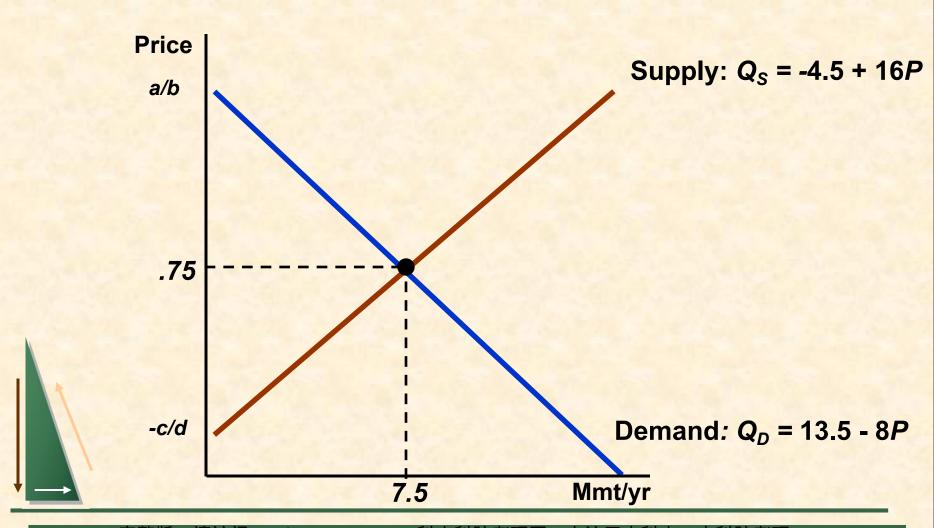
$$a = 13.5$$

$$Q = 13.5 - 8P$$

Setting supply equal to demand gives:

Supply = 
$$-4.5 + 16p = 13.5 - 8p = Demand$$
  
 $16p + 8p = 13.5 + 4.5$ 

$$p = 18/24 = .75$$



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- We have written supply and demand so that they only depend upon price.
- Demand could also depend upon income.
- Demand would then be written as:

$$Q = a - bP + fI$$

- We know the following information regarding the copper industry:
  - $\bullet$  | = 1.0
  - $P^* = 0.75$
  - $Q^* = 7.5$
  - b = 8
  - Income elasticity: E = 1.3

f can be found by substituting known values into the income elasticity formula:

$$E = (I/Q)(\Delta Q/\Delta I)$$
and
$$f = \Delta Q/\Delta I$$

Solving for f gives:

$$1.3 = (1.0/7.5)f$$
$$f = (1.3)(7.5)/1.0 = 9.75$$

Solving for a gives:

$$Q^* = a - bP^* + fI$$

$$7.5 = a - 8(0.75) + 9.75(1.0)$$

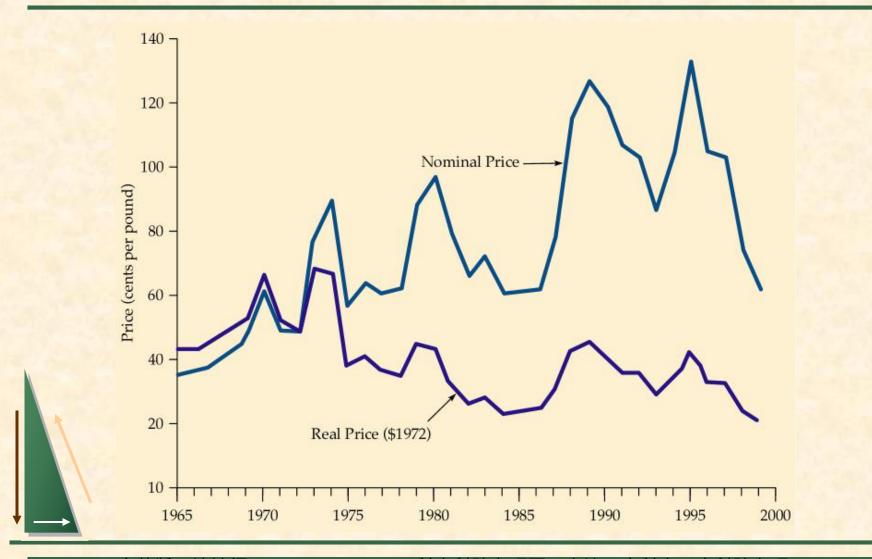
$$a = 3.75$$

# Declining Demand and the Manager Copper Prices Behavior of Copper Prices

- The relevant factors leading to a decrease in the demand for copper are:
  - 1) A decrease in the growth rate of power generation
  - 2) The development of substitutes: fiber optics and aluminum

### 

#### **Prices of Copper 1965 - 1999**



#### 

- We will try to estimate the impact of a 20 percent decrease in the demand for copper.
- Recall the equation for the demand curve:

$$Q = 13.5 - 8P$$

#### **Prices of Copper 1965 - 1999**

Multiply this equation by 0.80 to get the new equation. This gives:

$$Q = (0.80)(13.5 - 8P)$$

$$Q = 10.8 - 6.4P$$

Recall the equation for supply:

$$Q = -4.5 + 16P$$

#### 

■ The new equilibrium price is:

$$-4.5 + 16P = 10.8 - 6.4P$$

$$-16P + 6.4P = 10.8 + 4.5$$

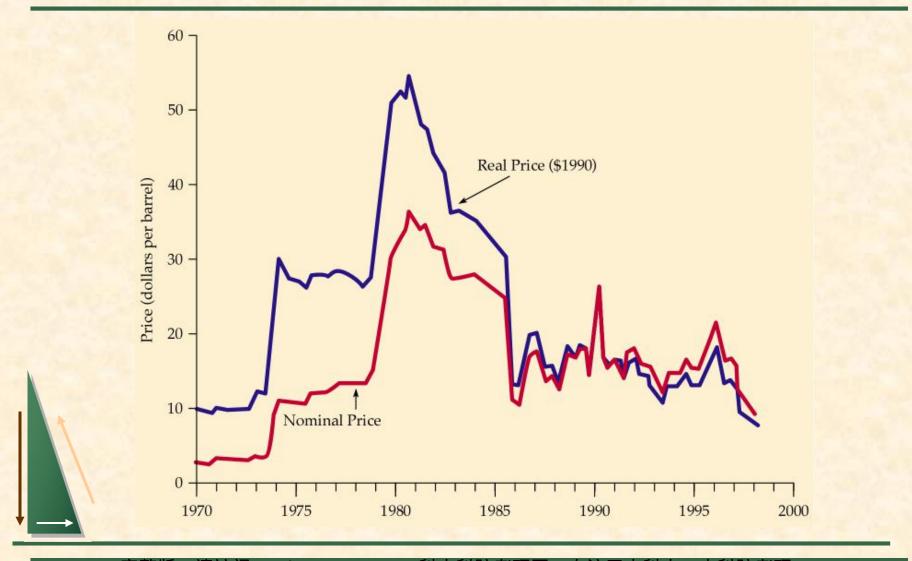
$$P = 15.3/22.4$$

### 

The twenty percent decrease in demand resulted in a reduction in the equilibrium price to 68.3 cents from 75 cents, or 10 percent.



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- We can predict numerically the impact of a decrease in the supply of OPEC oil.
- In 1995:
  - P\* = \$18/barrel
  - World demand and total supply = 23 bb/yr.
  - OPEC supply = 10 bb/yr.
  - Non-OPEC supply = 13 bb/yr

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#### Short-Run Long-Run

World Demand:

-0.05

-0.40

Competitive Supply (non-OPEC)

0.10

0.40

- Short-Run Impact of a stoppage of Saudi Production equal to 3 bb/yr.
  - Short-run Demand
    - D = 24.08 0.06P
  - Short-run Competitive Supply
    - $\bullet S_C = 11.74 + 0.07P$



- Short-Run Impact of a stoppage of Saudi Production equal to 3 bb/yr.
  - Short-run Total Supply--before supply reduction (includes OPEC, 10bb/yr)

$$\bullet S_T = 21.74 + 0.07P$$

Short-run Total Supply--after supply reduction

$$\bullet S_T = 18.74 + 0.07P$$

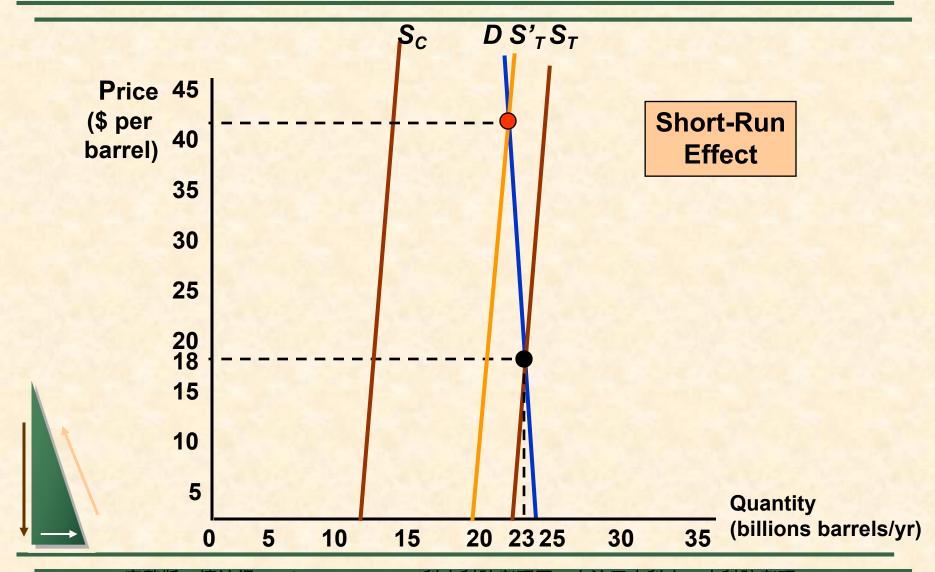
New Price After Reduction

$$24.08 - 0.06P = 18.74 + 0.07P$$

$$P = 41.08$$



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- Long-Run Impact of a stoppage Saudi Production equal to 3 bb/yr..
  - Long-run Demand
    - D = 32.18 0.51P
  - Long-run Total Supply
    - $\bullet$ S = 17.78 + 0.29P

New Price is found setting long-run supply equal to long-run demand:

$$32.18 - 0.51P = 14.78 + 0.29P$$

$$P = 21.75$$

